

**Lesson 3-1** Solving Two-Step Equations

<b>Lesson Objectives</b>	<b>NAEP 2005 Strand: Algebra: Equations</b>
<ul style="list-style-type: none"> <li>▼ Solve two-step equations</li> <li>▼ Use deductive reasoning</li> </ul>	<b>Topics: Equations and Inequalities; Mathematical Reasoning</b> <b>Local Standards:</b>

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**Key Concepts**

**Solving Two-Step Equations**

**Step 1** Use the Addition or Subtraction Property of Equality to get the term with a variable alone on one side of the equation.

**Step 2** Use the Multiplication or Division Property of Equality to write an equivalent equation in which the variable has a coefficient of 1.

$$\begin{array}{l}
 3x = 12 \\
 \frac{3x}{3} = \frac{12}{3} \\
 1x = 4 \\
 x = 4
 \end{array}$$

$$\begin{array}{l}
 x - 7 = 9 \\
 +7 \quad +7 \\
 \hline
 1x = 16 \\
 x = 16
 \end{array}$$

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**Key Concepts**

**Steps for Solving a Multi-Step Equation**

- Step 1 Clear the equation of fractions and decimals.
- Step 2 Use the Distributive Property to remove parentheses on each side.
- Step 3 Combine like terms on each side.
- Step 4 Undo addition or subtraction.
- Step 5 Undo multiplication or division.

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Solve  $21 = -p + 8$  p. 41

$$\begin{array}{l}
 21 = -p + 8 \\
 -8 \quad -8 \\
 \hline
 13 = -p \\
 -13 = -p \\
 (-1)13 = 1p(-1) \\
 -13 = p \\
 -x = 7 \quad -x = -2 \\
 x = -7 \quad x = 2
 \end{array}$$

$21 = -p + 8$   
 $21 = -(13) + 8$   
 $21 = 13 + 8$   
 $21 = 21 \checkmark$

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a.  $7 = 2y - 3$

$$\begin{array}{l}
 7 = 2y - 3 \\
 +3 \quad +3 \\
 \hline
 10 = 2y \\
 \frac{10}{2} = \frac{2y}{2} \\
 5 = y
 \end{array}$$

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b.  $\frac{x}{9} - 15 = 12$

$$\begin{array}{l}
 \frac{x}{9} - 15 = 12 \\
 +15 \quad +15 \\
 \hline
 \frac{x}{9} = 27 \\
 9 \cdot \frac{x}{9} = 9 \cdot 27 \\
 x = 243
 \end{array}$$

☺  $x = 243$

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c.  $-x + 15 = 12$

$$\begin{array}{r|l} -x + 15 & = 12 \\ -15 & -15 \\ \hline -x & = -3 \end{array}$$

$(-1) \cdot (-x) = -3 \cdot (-1)$

$$\begin{array}{r|l} -x & = -3 \\ (-1) & (-1) \\ \hline x & = 3 \end{array}$$

$x = 3$

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ex. 3 p. 42

Solve  $3 - 5z = 18$

~~$3 - 5z$~~   $-5z = 15$  Subtraction Prop.

$-5z = 15$  Simplify

$\frac{-5z}{-5} = \frac{15}{-5}$  Division Prop.

$z = -3$  Simplify

Quick v# 3

$$\begin{array}{r|l} -9 - 4m & = 3 \\ +9 & +9 \\ \hline -4m & = 12 \end{array}$$

Addition Prop.

$\frac{-4m}{-4} = \frac{12}{-4}$  Simplify

$m = -3$  Division Prop.

$m = -3$  Simplify

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$3 \cdot 21 + 6 + 21$

Solve  $3a + 6 + a = 90$  p. 43

$$\begin{array}{r|l} 4a + 6 & = 90 \\ -6 & -6 \\ \hline 4a & = 84 \\ \frac{4a}{4} & = \frac{84}{4} \\ a & = 21 \end{array}$$

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1. Solve each equation. p. 43

a.  $3x - 4x + 6 = -2$

$$\begin{array}{r|l} -x + 6 & = -2 \\ -6 & -6 \\ \hline -x & = -8 \\ \frac{-x}{-1} & = \frac{-8}{-1} \\ x & = 8 \end{array}$$

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b.  $7 = 4m - 2m + 1$  p. 43

$$\begin{array}{r|l} 7 & = 2m + 1 \\ -1 & -1 \\ \hline 6 & = 2m \\ \frac{6}{2} & = \frac{2m}{2} \\ 3 & = m \end{array}$$

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~~\*~~

c.  $-2y + 5 + 5y = 14$  p. 43

$$\begin{array}{r|l} 3y + 5 & = 14 \\ -5 & -5 \\ \hline 3y & = 9 \\ \frac{3y}{3} & = \frac{9}{3} \\ y & = 3 \end{array}$$

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**d.**  $-3z + 8 + (-2z) = -12$  p. 43

$$\begin{array}{r} -5z + 8 = -12 \\ -8 \quad -8 \\ \hline -5z = -20 \\ \frac{-5}{-5} \quad \frac{-5}{-5} \\ z = 4 \end{array}$$

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p. 44

Solve  $2(x - 3) = 8$

$$\begin{array}{r} 2 \cdot x - 2 \cdot 3 = 8 \\ 2x - 6 = 8 \\ \quad +6 \quad +6 \\ \hline 2x = 14 \\ \frac{2}{2} \quad \frac{14}{2} \\ x = 7 \end{array}$$

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Solve  $\frac{3x}{2} + \frac{x}{5} = 17$

multiply every term by the LCD. LCD=10

$$\begin{array}{r} 10 \cdot \frac{3x}{2} + 10 \cdot \frac{x}{5} = 10 \cdot 17 \\ 15x + 2x = 170 \\ 17x = 170 \\ \frac{17x}{17} = \frac{170}{17} \\ x = 10 \end{array}$$

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Solve each equation.

3. a.  $3(k + 8) = 21$

$$\begin{array}{r} 3 \cdot k + 3 \cdot 8 = 21 \\ 3k + 24 = 21 \\ \quad -24 \quad -24 \\ \hline 3k = -3 \\ \frac{3k}{3} = \frac{-3}{3} \\ k = -1 \end{array}$$

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b.  $15 = -3(x - 1) + 9$

$$\begin{array}{r} 15 = -3 \cdot x - 3 \cdot 1 + 9 \\ 15 = -3x + 3 + 9 \\ 15 = -3x + 12 \\ \quad +12 \quad +12 \\ \hline 3 = -3x \\ \frac{3}{-3} = \frac{-3x}{-3} \\ -1 = x \end{array}$$

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a.  $\frac{m}{4} + \frac{m}{2} = \frac{5}{8}$

$$\begin{array}{r} \frac{2}{2} \cdot \frac{m}{4} + \frac{4}{4} \cdot \frac{m}{2} = \frac{5}{8} \\ \frac{2m}{4} + \frac{4m}{4} = \frac{5}{8} \\ 2m + 4m = 5 \\ 6m = 5 \\ \frac{6m}{6} = \frac{5}{6} \\ m = \frac{5}{6} \end{array}$$

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