

**Check Skills You'll Need** 0:00:00

**Find the common difference of each sequence.**

1. 1, 3, 5, 7, ... 2

2. 19, 17, 15, 13, ... -2

3. 1.3, 0.1, -1.1, -2.3, ... -2

4. 18, 21.5, 25, 28.5, ... 3.5

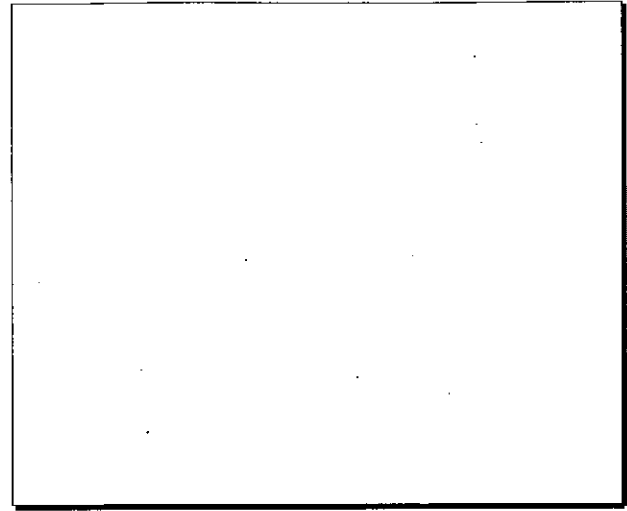
**Use inductive reasoning to find the next two numbers in each pattern.**

5. 2, 4, 8, 16, ... 32, 64

6. 4, 12, 36, ...  $\frac{12}{4} = 3$  108, 324

7. 0.2, 0.4, 0.8, 1.6, ... 3.2, 6.4

8. 200, 100, 50, 25, ...  $\frac{36}{12} = 3$   
= 12.5  
= 6.25



**Day 70**

**Lesson 8-6** Geometric Sequences

<b>Lesson Objectives</b> ▼ Form geometric sequences ▼ Use formulas when describing geometric sequences	<b>NAEP 2005 Strand: Algebra</b> Topic: Patterns, Relations, and Functions Local Standards: _____
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**Vocabulary and Key Concepts**

Geometric Sequence	Rule	Geometric Sequence
	$A(n) = a \cdot r^{n-1}$	
	↑     ↑     ↓ nth first common term term term ratio	

has

A geometric sequence ~~x~~ **A ratio between consecutive terms is constant.**

A common ratio is **the ratio between the consecutive terms.**

**Arithmetic:** add/subtract to get the next term  
 3, 5, 7, 9, ...  $d = 2$

**Geometric:** multiply or ÷ to get the next term  
 10, 20, 40, 80, ...  $r = 2$

$r = \frac{20}{10} = 2$      $r = \frac{40}{20} = 2$

**1 Finding the Common Ratio** Find the common ratio of each sequence.

a. 3, -15, 75, -375, ...

1 2 3 4      2 3 4  
 $\frac{2}{1}$     $\frac{3}{2}$     $\frac{4}{3}$

3      -15      75      -375

$\times (-5) \times (-5) \times (-5)$

$\frac{-15}{3} = -5$        $\frac{75}{-15} = -5$        $\frac{-375}{75} = -5$

The common ratio is  $-5$ .

$r = -5$

**1 Finding the Common Ratio** Find the common ratio of each sequence.

h.  $3, \frac{3}{2}, \frac{3}{4}, \frac{3}{8}, \dots$

1 2 3  
 $\frac{2}{1}$     $\frac{3}{2}$     $\frac{3}{8}$

3       $\frac{3}{2}$        $\frac{3}{4}$        $\frac{3}{8}$

$\times \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2}$

The common ratio is  $\frac{1}{2}$       3rd  $\div$  2nd

$\frac{3}{2} \div \frac{3}{4} = \frac{3}{2} \cdot \frac{4}{3} = 2$

$\frac{3}{4} \div \frac{3}{8} = \frac{3}{4} \cdot \frac{8}{3} = 2$

$\frac{3}{8} \div \frac{3}{16} = \frac{3}{8} \cdot \frac{16}{3} = 2$

$\frac{2}{4} = \frac{1}{2}$

**1. Find the common ratio of each sequence.**

a. 750, 150, 30, 6, ...      b. -3, -6, -12, -24, ...      c. 4, 6, 9, 13.5, ...

$r = \frac{1}{5}$        $r = 2$        $r = 1.5$   
 $r = \frac{3}{2}$

$\frac{2}{1} \frac{150}{750} = \frac{1}{5}$        $\frac{3}{2} \frac{30}{150} = \frac{1}{5}$        $\frac{-6}{-3} = 2$        $\frac{6}{4} = 1.5$   
 $\frac{6}{9} = 1.5$        $\frac{9}{6} = 1.5$        $\frac{-12}{-6} = 2$        $\frac{13.5}{9} = 1.5$   
 $\frac{18}{13.5} = 1.33$        $\frac{-24}{-12} = 2$        $\frac{18}{13.5} = 1.33$

**2 Arithmetic or Geometric Sequence** Determine whether each sequence is arithmetic or geometric.

a. 162, 54, 18, 6, ...

$\frac{54}{162} = \frac{1}{3} = \frac{1}{3}$

162      54      18      6       $\frac{18}{54} = \frac{1}{3}$

$\times \frac{1}{3} \times \frac{1}{3} \times \frac{1}{3}$

The sequence has a ratio of  $\frac{1}{3}$ .

ratio: The sequence is geometric.

2 Arithmetic or Geometric Sequence Determine whether each sequence is arithmetic or geometric.

b. 98, 101, 104, 107, ...

$$\begin{array}{cccc} & & \frac{101}{-98} & \frac{104}{-101} \\ & & \frac{3}{3} & \frac{3}{3} \\ 98 & 101 & 104 & 107 \\ \swarrow & \swarrow & \swarrow & \\ +3 & +3 & +3 & \end{array}$$

The sequence has a  $d=3$  common difference difference. The sequence is Arithmetic.

3 Finding Terms of a Sequence Find the first, fifth, and tenth terms of the sequence that has the rule  $A(n) = -3(2)^{n-1}$ .

first term:  $A(1) = -3(2)^{1-1} = -3(2)^0 = -3(1) = -3$

fifth term:  $A(5) = -3(2)^{5-1} = -3(2)^4 = -3(16) = -48$

tenth term:  $A(10) = -3(2)^{10-1} = -3(2)^9 = -3(512) = -1536$

**Quick Check**

2. Determine whether each sequence is arithmetic or geometric.

a. 2, 4, 6, 8, ... b. 2, 4, 8, 16, ...

A  $d=+2$

$\ominus$   $r=2$

c. 1, 3, 5, 7, ...

A  $d=+2$

3. Find the first, sixth, and twelfth terms of each sequence.

a.  $A(n) = 4 \cdot 3^{n-1}$  b.  $A(n) = -2 \cdot 5^{n-1}$

first: 4 ✓

sixth: 972 ✓

twelfth: ~~768, 588~~

$4 \cdot 3^{1-1} = 4 \cdot 3^0 = 4 \cdot 1 = 4$   
 $4 \cdot 3^{6-1} = 4 \cdot 3^5$   
 $4 \cdot 3^{12-1} = 4 \cdot 3^{11}$

$$2 \text{ meters} = \underline{200} \text{ cm}$$

$$A(n) = a \cdot r^{n-1}$$

$$A(n) = 200(.75)^{n-1}$$

$$r = 75\% = .75 \quad A(3) = 200(.75)^{3-1}$$

$$= 200(.75)^2$$

$$= 112.5$$

1 Find the common ratio of each sequence.

a. 750, 150, 30, 6, ...

b. -3, -6, -12, -24, ...

c. 4, 6, 9, 13.5, ...

2 Find the next three terms of each sequence.

a. 1, 3, 9, 27, ...

b. 120, -60, 30, -15, ...

c. 1.1, 2.2, 4.4, 8.8, ...

3 Determine whether each sequence is arithmetic or geometric.

a. 2, 4, 6, 8, ...

b. 2, 4, 8, 16, ...

c. 1, 3, 5, 7, ...

- 4 Find the first, sixth, and twelfth terms of each sequence.  
 a.  $A(n) = 4 \cdot 3^{n-1}$                       b.  $A(n) = -2 \cdot 5^{n-1}$

$A(n) = a \cdot r^{n-1}$

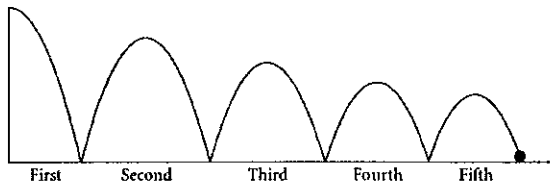
Write a rule and find the given term in each geometric sequence described below.

25. What is the fifth term when the first term is 6 and the common ratio is 0.5?  
 $A(5) = 6 \cdot (.5)^{5-1}$

26. What is the tenth term when the first term is -6 and the common ratio is 2?  
 $A(10) = -6 \cdot (2)^{10-1}$

27. What is the fourth term when the first term is 7 and the common ratio is 1.1?

**Sports** You drop a rubber ball from a height of 1 meter and it bounces back to lower and lower heights. Each curved path has 80% the height of the previous path. Write a rule for the height of each successive path. What height will the ball reach at the top of the fifth path?  
 Draw a diagram to help understand the problem.



The height of the first path is 100 cm. So the height is 100 cm for the first term, with  $n = 1$ . The height of the fifth path is given by the term  $n = 5$ . The common ratio is 80%, or 0.8.

A rule for the sequence is  $A(n) = 100 \cdot 0.8^{n-1}$ .

$A(n) = 100 \cdot 0.8^{n-1}$     Use the sequence to find the height of the fifth path.  
 $A(5) = 100 \cdot 0.8^{5-1}$     Substitute 5 for  $n$ .  
 $= 100 \cdot 0.8^4$             Simplify exponents.  
 $= 100 \cdot 0.4096$         Evaluate powers.  
 $= 40.96$                     Simplify.

The height of the fourth bounce will be 40.96 cm.

Name

B1 12/10

WRBK p.399 (8.6)

1.

2.

3.

4.

5.

6.

11.

12.

13.

14.

15.

16.

17.

18.

27

28

36

37