

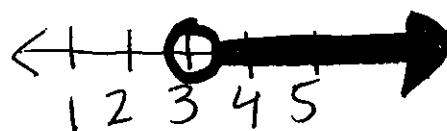
1.4 Solving Inequalities (\mathbb{R} #'s)

these rules only apply if the variable is left

$\left\{ \begin{array}{l} <, \leq \text{ shade left (less thans)} \\ >, \geq \text{ shade right (greater thans)} \end{array} \right.$

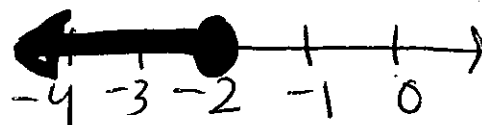
(ex) $<, >$ open circle

$x > 3$



(ex) \leq, \geq closed circle

$y \leq -2$



An inequality can have many solutions, all real #'s, or NO solution.

★ If you divide or multiply by a negative #, the inequality sign flips! ★

$-1(5) > (-2) - 1$

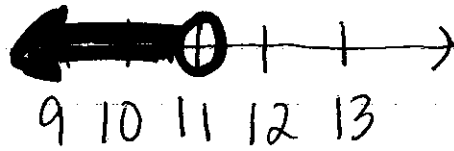
$-5 > 2$ False

$-5 < 2$ True

Solve + Graph

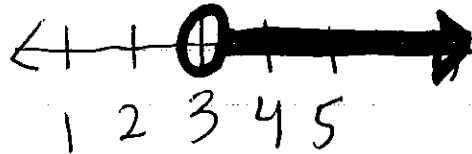
①

$$\begin{array}{r|l}
 3x - 6 < 27 \\
 +6 & +6 \\
 \hline
 3x < 33 \\
 \frac{3x}{3} & \frac{33}{3} \\
 \hline
 x < 11
 \end{array}$$



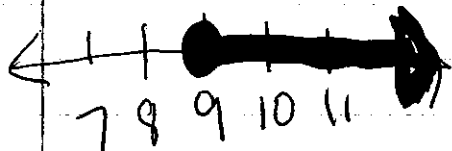
ex

$$\begin{array}{r|l}
 -2x < 3(x - 5) \\
 -2x < 3x - 15 \\
 -3x & -3x \\
 \hline
 -5x < -15 \\
 \frac{-5x}{-5} & \frac{-15}{-5} \\
 \hline
 x > 3
 \end{array}$$



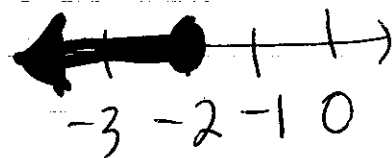
ex

$9 \leq x \rightarrow$ this means $x \geq 9$
greater than or = to



ex

$$\begin{array}{r}
 12 \geq 2(3n + 1) + 22 \\
 12 \geq 6n + 2 + 22 \\
 12 \geq 6n + 24 \\
 \frac{12}{6} \geq \frac{6n}{6} \quad \frac{-24}{6} \\
 2 \geq n \quad -24 \geq 6n - 24 \\
 \frac{-24}{6} \geq \frac{6n}{6} \quad -24 \geq 6n - 24 \\
 \hline
 -2 \geq n
 \end{array}$$



$n \leq -2$

(ex)

$$2x < 2(x+1) + 3$$

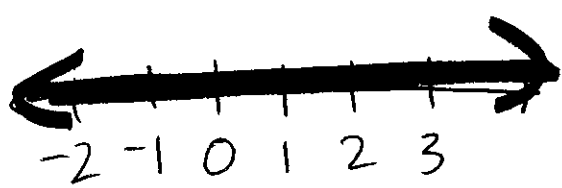
$$2x < 2x + 2 + 3$$

$$\begin{array}{r} 2x < 2x + 5 \\ -2x \quad -2x \\ \hline \end{array}$$

$$0 < 5 \text{ true}$$

* if variables cancel + you get a true statement, then x can be any real #

All \mathbb{R} #'s



↑ answer ↑ answer

(ex)

$$4(x-3) + 7 \geq 4x + 1$$

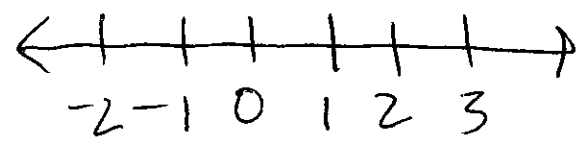
$$4x - 12 + 7 \geq 4x + 1$$

$$\begin{array}{r} 4x - 5 \geq 4x + 1 \\ -4x \quad -4x \\ \hline \end{array}$$

$-5 \geq 1$ False statement = No solution

\emptyset

OR



No shading on the # line

FIVE STAR

FIVE STAR

FIVE STAR

FIVE STAR

FIVE STAR

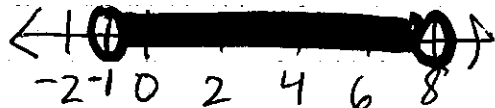
Compound Inequality

(ex)

$$\begin{array}{ccc} -6 < 2x - 4 < 12 \\ +4 & & +4 \end{array}$$

$$\begin{array}{ccc} -2 < \frac{2x}{2} < \frac{16}{2} \\ 2 & & 2 \end{array}$$

$$-1 < x < 8$$



(x is between -1 and 8)

(ex)

$$3x + 9 < -3 \quad \underline{\underline{\text{OR}}} \quad -2x + 1 < 5$$

$$\begin{array}{ccc} 3x < -12 \\ \frac{3}{3} & & \frac{-12}{3} \end{array}$$

$$x < -4$$

$$\begin{array}{ccc} -2x < 4 \\ \frac{-2x}{-2} & & \frac{4}{-2} \end{array}$$

$$x > -2$$

