

Day 68

7.1 Roots and Radical Expressions

$$5^2 = 25 \rightarrow \sqrt{25} = 5$$

$$5^3 = 125 \rightarrow \sqrt[3]{125} = 5$$

$$5^4 = 625 \rightarrow \sqrt[4]{625} = 5$$

$$4 \sqrt[4]{\boxed{\text{math}} \boxed{5}} \quad 4 \sqrt{\quad}$$

$$\sqrt{-25} \text{ undefined}$$

$$\sqrt[3]{-125} = -5$$

 25 -5
 -5 -5

you can take the odd root of negative #'s.

$$\sqrt[5]{-32} = -2$$

you can't take the even root of a negative #

$$\sqrt[4]{-16} \text{ undefined}$$

When you take the even root of a positive # there are 2 solutions (\pm)

For any negative #

$$\text{even } \rightarrow \sqrt[n]{a^n} = |a| \text{ when } n \text{ is even}$$

↑
the root

abs. value bars are for the variables

Practice 7-1

Roots and Radical Expressions

Find each real-number root.

1. $\sqrt{144}$

12

2. $-\sqrt{25}$

-5

3. $\sqrt{-0.01}$

undefined

4. $\sqrt[3]{0.001}$

.1

5. $\sqrt[4]{0.0081}$

.3

6. $\sqrt[3]{27}$

3

7. $\sqrt[3]{-27}$

-3

8. $\sqrt{0.09}$

.3

Find all the real cube roots of each number.

9. 216

$\sqrt[3]{216} = 6$

10. -343

$\sqrt[3]{-343} = -7$

11. -0.064

-0.4

12. $\sqrt[3]{\frac{1000}{27}} = \frac{10}{3}$

Find all the real square roots of each number.

13. 400

$\sqrt{400} = \pm 20$

14. $\sqrt{-196}$

undefined

15. 10,000

± 100

16. 0.0625

± 0.25

even roots (\pm)

Find all the real fourth roots of each number.

17. $\sqrt[4]{-81}$

undefined

18. $\sqrt[4]{256}$

± 4

19. $\sqrt[4]{0.0001}$

± 0.1

20. $\sqrt[4]{625}$

± 5

Simplify each radical expression. Use absolute value symbols when needed.

21. $\sqrt{81x^4}$

$9 \cdot 9 \cdot x \cdot x$
 $9x \cdot x$
 $= 9x^2$

22. $\sqrt{121y^{10}}$

$11 \cdot 11$
 $11 | y^5 |$

23. $\sqrt[3]{8g^6}$

$2 \cdot 2 \cdot 2$
 $2g^2$

24. $\sqrt[3]{125x^9}$

$5 \cdot 5 \cdot 5$
 $5x^3$

44444
44444
44444

XXXXXX

$$\sqrt[3]{(x-9)(x-9)(x-9)}$$

$$15 \div 5 = 3$$

25. $\sqrt[5]{243x^5y^{15}}$

26. $\sqrt[3]{(x-9)^3}$

27. $\sqrt{25(x+2)^4}$

28. $\sqrt[3]{\frac{64x^9}{343}}$ $9 \div 3$

$3xy^3$

$x-9$

$5(x+2)^2$

$= \frac{4x^3}{7}$

Find the two real-number solutions of each equation.

29. $\sqrt{x^2} = \sqrt{4}$

30. $\sqrt[4]{x^4} = \sqrt[4]{81}$

31. $\sqrt{x^2} = \sqrt{0.16}$

32. $\sqrt{x^2} = \sqrt{\frac{16}{49}}$

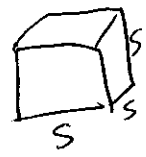
$x = \pm 2$

$x = \pm 3$

$\pm .4$

$x = \pm \frac{4}{7}$

33. A cube has volume $V = s^3$, where s is the length of a side. Find the side length for a cube with volume 8000 cm^3 .



$$\sqrt[3]{8000} = \sqrt[3]{s^3}$$

$20 \text{ cm} = s$

34. The velocity of a falling object can be found using the formula $v^2 = 64h$, where v is the velocity (in feet per second) and h is the distance the object has already fallen.

a. What is the velocity of the object after a 10-foot fall?

$$v^2 = 64(10)$$

$$\sqrt{v^2} = \sqrt{640}$$

$v \approx 25.3 \text{ ft/sec}$

b. How much does the velocity increase if the object falls 20 feet rather than 10 feet?

$$v^2 = 64(20)$$

$$v^2 = 1280$$

$$v \approx 35.8 \text{ ft/sec}$$

$\approx 10.5 \text{ ft sec}$