

10.4 Ellipses with center at (h, k)

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

major axis (x)

b^2

$a^2 \leftarrow y$ major axis

ex1)
$$\frac{(x-3)^2}{9} + \frac{(y+4)^2}{16} = 1$$

center: $(3, -4)$ major (y)

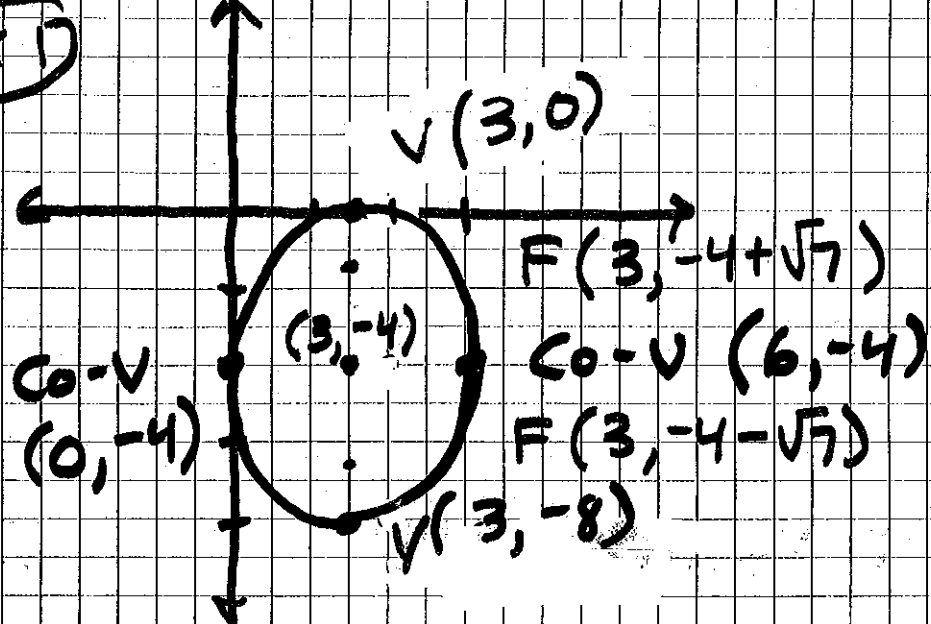
$a = 4$
 $b = 3$

$$c^2 = a^2 - b^2$$
$$c^2 = 16 - 9$$
$$\sqrt{c^2} = \sqrt{7}$$
$$c = \pm\sqrt{7}$$

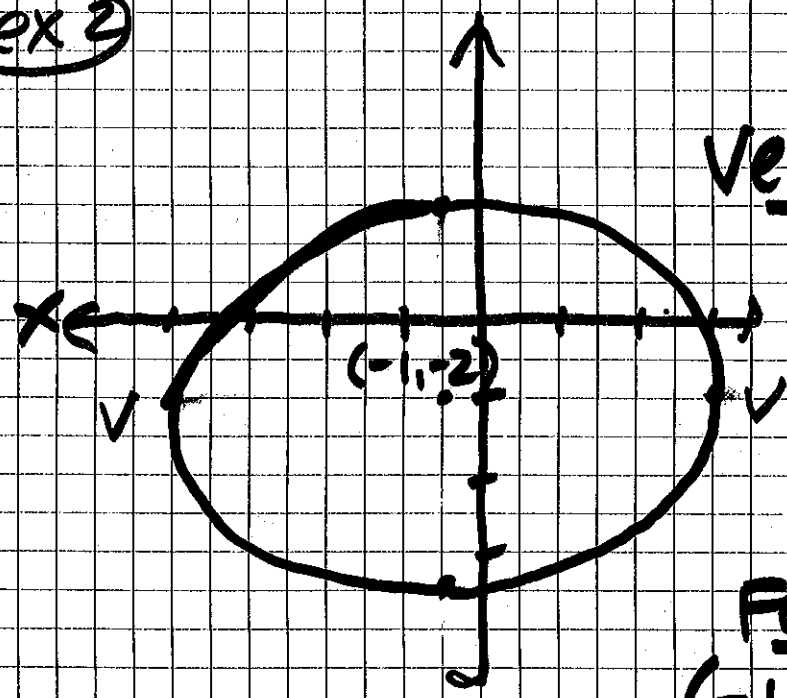
ex2)
$$\frac{(x+1)^2}{49} + \frac{(y+2)^2}{25} = 1$$

$(-1, -2)$ $c^2 = 49 - 25 = \sqrt{24}$
 $\sqrt[4]{6}$

$a = 7$ $c = 2\sqrt{6}$
 $b = 5$



(ex 2)



Vertices: $(-8, -2)$
 $(6, -2)$

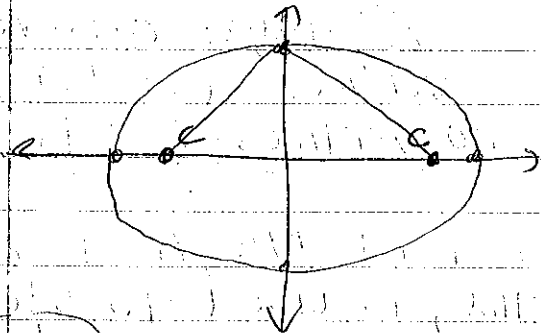
Co-vertices:
 $(-1, -7)$ $(-1, 3)$

Foci:
 $(-1 + 2\sqrt{6}, -2)$
 $(-1 - 2\sqrt{6}, -2)$

x
 value \uparrow center
 add + subtract
 "c" from it

The Foci are important points in an ellipse. For example, in Earth's orbit around the sun, the sun is at a FOCUS, not at the center.

- the foci of an ellipse are always on the major axis and are c units from the center.



$$c^2 = a^2 - b^2$$

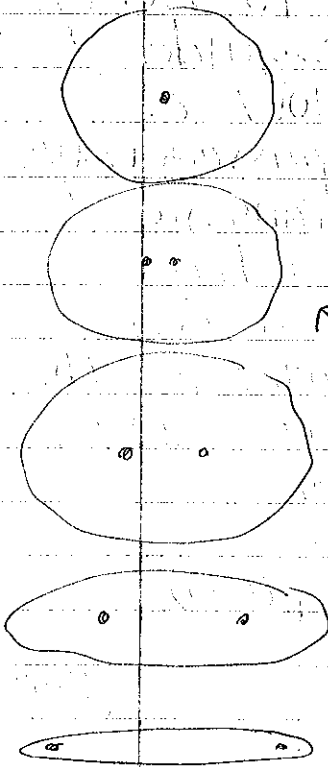
$$c = \sqrt{a^2 - b^2}$$

The eccentricity of an ellipse is a measure of its ovalness.

It is given by $\frac{c}{a}$

IF an ellipse is nearly circular
 - the foci are close to the center
 the eccentricity,
 given by $\frac{c}{a}$ is close to 0.

IF the ellipse is very elongated
 then the foci are close to the
 vertices and the eccentricity is
 close to 1.



Ellipses day 3

3/8

⊗ $25x^2 + 16y^2 + 150x = 160y - 225$

$25x^2 + 150x + 16y^2 - 160y = -225$

$25(x^2 + 6x + 9) + 16(y^2 - 10y + 25) = -225 + 25(9) + 16(25)$

$\frac{25(x+3)^2}{400} + \frac{16(y-5)^2}{400} = \frac{400}{400}$

$\frac{(x+3)^2}{16} + \frac{(y-5)^2}{25} = 1$

b^2
 $b = 4$

a^2
 $a = 5$

major: y
 center: $(-3, 5)$

$c^2 = a^2 - b^2$

vertices: $(-3, 10)$
 $(-3, 0)$

$c^2 = 25 - 16$

co-vertices: $(-7, 5)$
 $(1, 5)$

$\sqrt{c^2} = \sqrt{9}$

$c = 3$

Foci:

$(-3, 8)$ $(-3, 2)$

eccentricity: $\frac{3}{5} = .6$

$$2x^2 + 8x + y^2 + 4 = 0$$

$$2x^2 + 8x + y^2 = -4$$

$$2(x^2 + 4x + \boxed{4}) + y^2 = -4 + \boxed{8}$$

$$\frac{2(x+2)^2}{4} + \frac{y^2}{4} = \frac{4}{4}$$

$$\frac{(x+2)^2}{2^2} + \frac{y^2}{2^2} = 1$$

Center:
 $(-2, 0)$

major y

$$a = 2$$

vertices:

$$(-2, 2) \quad (-2, -2)$$

co-vertices:

$$(-2 \pm \sqrt{2}, 0)$$

$$\text{Foci } (-2, \pm\sqrt{2})$$

$$c^2 = a^2 - b^2$$

$$\sqrt{c^2} = \sqrt{4 - 2}$$
$$c = \sqrt{2}$$

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c
Ho

Name _____

Ellipses

Put each ellipse in standard form if necessary. Find the pertinent information. Sketch the graph.

$$1.) \frac{x^2}{25} + \frac{y^2}{16} = 1$$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

$$2.) \frac{x^2}{36} + \frac{y^2}{20} = 1$$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

$$3.) \frac{(x+5)^2}{9} + \frac{(y-3)^2}{3} = 1$$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

$$4.) 169x^2 + 25y^2 = 4225$$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

$$5.) 9x^2 + 25y^2 + 72x - 150y = -144$$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

Name _____

Ellipses

6.) $x^2 + 4y^2 - 2x + 24y + 33 = 0$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

7.) $9x^2 + 16y^2 = 144$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

8.) $9x^2 + 25y^2 + 54x + 200y = -256$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____

9.) $4x^2 + y^2 - 32x - 4y + 52 = 0$

Major axis: _____

Vertices: _____

Co-vertices: _____

Foci: _____

Center: _____

eccentricity: _____