

We learned how to find area and circumference. See if you can work backwards to find radius, diameter, circumference...

1. If $A = 9\pi \text{ cm}^2$

Find the radius & Circumference.

$$\frac{9\pi}{\pi} = \frac{4\pi r^2}{\pi}$$

$$C = 2\pi r$$

$$C = 2 \cdot \pi \cdot 3$$

$$C = 6\pi \text{ cm}$$

$$\sqrt{9} = \sqrt{r^2} \quad r = 3$$



2. If $A = 3\pi \text{ cm}^2$

Find the diameter.

Find the radius and then double it

$$\text{Area} = 4\pi r^2$$

$$\frac{3\pi}{\pi} = \frac{4\pi r^2}{\pi}$$

$$\sqrt{3} = \sqrt{r^2}$$

$$\sqrt{3} = r$$

$$\approx 1.732$$

$$\times 2$$

$$d = 3.46 \text{ cm}$$

1st: \div by π on both sides

2nd: take the $\sqrt{\quad}$ of both sides

Feb 4-3:01 PM

3. If $C = 10\pi \text{ cm}$

Find the Area.

$$C = 2\pi r$$

$$\frac{10\pi}{2\pi} = \frac{2\pi r}{2\pi}$$

\div by 2π

$$5 = r$$

$$A = \pi \cdot 5^2$$

$$A = 25\pi \text{ cm}^2$$



4. If $A = 8 \text{ cm}^2$

Find the diameter.

$$A = \pi r^2$$

$$\frac{8}{\pi} = \frac{\pi r^2}{\pi}$$

$$\sqrt{2.546} = \sqrt{r^2}$$

$$1.5957 = r$$

$\times 2$

$$3.19 = d$$

Feb 4-3:02 PM

5. $C = 314 \text{ m}$
 $A = \underline{\hspace{2cm}}$

$$C = 2\pi r$$

$$\frac{314}{2\pi} = \frac{2\pi r}{2\pi}$$

$$49.97 = r$$

when typing into the calculator put parentheses around 2π

$$A = \pi (49.97)^2$$

$$A = 2497.465856 \pi \text{ m}^2$$

so it looks like this

$$\rightarrow 314 \div (2\pi)$$

OR

$$A = 7846.02 \text{ m}^2$$

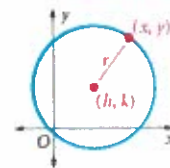
Feb 4-3:08 PM

12-5

Circles in the Coordinate Plane

1 Writing an Equation of a Circle

You can use the Distance Formula to find an equation of a circle with center (h, k) and radius r . Let (x, y) be any point on the circle. Then the radius r is the distance from (h, k) to (x, y) .



$$r = \sqrt{(x - h)^2 + (y - k)^2} \quad \text{Distance Formula}$$

$$r^2 = (x - h)^2 + (y - k)^2 \quad \text{Square both sides.}$$

This essentially proves the following theorem.

Key Concepts

Theorem 12-13

An equation of a circle with center (h, k) and radius r is $(x - h)^2 + (y - k)^2 = r^2$.

IF the center is at the origin $(0,0)$
 then you can use

$$x^2 + y^2 = r^2$$

Apr 24-3:20 PM

The equation $(x - h)^2 + (y - k)^2 = r^2$ is in **standard form**. You may also call it the *standard equation* of a circle.

1 EXAMPLE Writing the Equation of a Circle

Write the standard equation of the circle with center $(5, -2)$ and radius 7.

$(x - h)^2 + (y - k)^2 = r^2$ Use standard form.

$(x - 5)^2 + [y - (-2)]^2 = 7^2$ Substitute $(5, -2)$ for (h, k) , and 7 for r .

$(x - 5)^2 + (y + 2)^2 = 49$ Simplify.

1 Write the standard equation of each circle.

a. center $(3, 5)$; radius 6

$h=3$ $k=5$

$(x-3)^2 + (y-5)^2 = 6^2$

$(x-3)^2 + (y-5)^2 = 36$

b. center $(-2, -1)$; radius $\sqrt{2}$

$h=-2$ $k=-1$

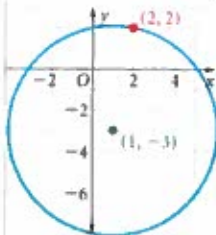
$(x-(-2))^2 + (y-(-1))^2 = (\sqrt{2})^2$

$(x+2)^2 + (y+1)^2 = 2$

Apr 24-3:22 PM

If you know the center of a circle and a point on the circle, you can write the standard equation of the circle.

2 EXAMPLE Using the Center and a Point on a Circle



Write the standard equation of the circle with center $(1, -3)$ that passes through the point $(2, 2)$.

$r = \sqrt{(x - h)^2 + (y - k)^2}$
 $= \sqrt{(2 - 1)^2 + (2 - (-3))^2}$
 $= \sqrt{1 + 25} = \sqrt{26}$

Use the Distance Formula to find r .

Substitute $(1, -3)$ for (h, k) , and $(2, 2)$ for (x, y) .

Simplify.

$(x - h)^2 + (y - k)^2 = r^2$

Use standard form.

$(x - 1)^2 + [y - (-3)]^2 = (\sqrt{26})^2$

Substitute $(1, -3)$ for (h, k) , and $\sqrt{26}$ for r .

$(x - 1)^2 + (y + 3)^2 = 26$

Simplify.

2 Write the standard equation of the circle with center $(2, 3)$ that passes through the point $(-1, 1)$.

$h=2$ $k=3$

$d = \sqrt{(2 - (-1))^2 + (3 - 1)^2}$

$d = \sqrt{3^2 + 2^2}$

$d = \sqrt{9 + 4}$

$d = \sqrt{13}$

so the radius is $\sqrt{13}$

$(x-2)^2 + (y-3)^2 = 13$

Apr 24-3:22 PM

use the distance formula to find the radius.

square the radius to put into eq.

2 Finding the Center and Radius of a Circle

If you know the standard equation of a circle, you can describe the circle by naming its center and radius. Then you can use this information to graph the circle.

3 EXAMPLE Graphing a Circle Given its Equation

Find the center and radius of the circle with equation $(x - 7)^2 + (y + 2)^2 = 64$.

$$(x - 7)^2 + (y + 2)^2 = 64$$

$$(x - 7)^2 + (y - (-2))^2 = 8^2 \quad \text{Use standard form.}$$

\uparrow \uparrow \uparrow
 h k r

The center is $(7, -2)$ and the radius is 8 .

3 Find the center and radius of the circle with equation $(x - 2)^2 + (y - 3)^2 = 100$.

\swarrow \searrow
 $x - 2 = 0$ $y - 3 = 0$
 $+2 +2$ $+3 +3$
 $x = 2$ $y = 3$
 SO center $(2, 3)$
 h k

\swarrow \searrow
 $\sqrt{100} = r$
 $10 = r$

100 is R^2
 square root to
 Find the radius

Apr 24-3:23 PM

★ Now combine Area & Circumference with Eqs. of Circles.

The equation of a circle in the coordinate plane with center $(0, 0)$ is $x^2 + y^2 = r^2$

r is the radius

Write the equation of the circle. Find C & A .

1st Find the radius: 6

eq: $x^2 + y^2 = 36$

$C = (0, 0)$

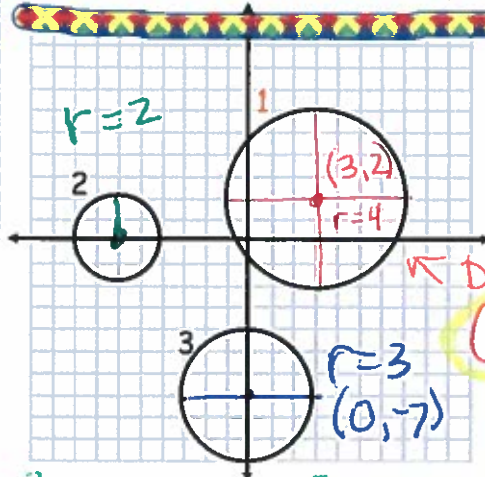
$A = 36\pi \text{ in}^2$

$A = \pi r^2$
 $= \pi \cdot 6^2$

remember this is r^2

Feb 4-2:56 PM

The equation of a circle in the coordinate plane with center (h, k) is $(x - h)^2 + (y - k)^2 = r^2$



center $(-6, 0)$

Write the equation of the circle. Find C & A .

1st: Determine the center and radius of each graph.

Draw diameters to find center

① $(x - 3)^2 + (y - 2)^2 = 16$

$C = 2 \cdot \pi \cdot 4$

$C = 8\pi \text{ un}$

$A = \pi r^2$

$A = 16\pi \text{ un}^2$

③ $(x - 0)^2 + (y - -7)^2 = 3^2$

$x^2 + (y + 7)^2 = 9$

$C = 2\pi \cdot 3$

$A = \pi \cdot 3^2$

$C = 6\pi \text{ un}$

$A = 9\pi \text{ un}^2$

② $(x - -6)^2 + (y - 0)^2 = 2^2$

$(x + 6)^2 + y^2 = 4$

$C = 2 \cdot \pi \cdot 2$ $A = \pi \cdot 2^2$

$C = 4\pi \text{ un}$

$A = 4\pi \text{ un}^2$

Feb 4-2:56 PM

example. $C = 2\pi$

Find the equation of the circle if the center is at $(-5, 6)$.

$C = 2\pi r$

$\frac{2\pi}{2\pi} = \frac{2\pi r}{2\pi}$

$1 = r$

$(x - -5)^2 + (y - 6)^2 = 1^2$

$(x + 5)^2 + (y - 6)^2 = 1$

Feb 8-12:45 PM

